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# A two-compartment mathematical model of neuroglial metabolism using [1-<sup>11</sup>C] acetate

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The purpose of this study was to develop a two-compartment metabolic model of brain metabolism to assess oxidative metabolism from [1-<sup>11</sup>C] acetate radiotracer experiments, using an approach previously applied in <sup>13</sup>C magnetic resonance spectroscopy (MRS), and compared with an one-tissue compartment model previously used in brain [1-<sup>11</sup>C] acetate studies. Compared with <sup>13</sup>C MRS studies, <sup>11</sup>C radiotracer measurements provide a single uptake curve representing the sum of all labeled metabolites, without chemical differentiation, but with higher temporal resolution. The reliability of the adjusted metabolic fluxes was analyzed with Monte-Carlo simulations using synthetic <sup>11</sup>C uptake curves, based on a typical arterial input function and previously published values of the neuroglial fluxes  $V_{1ca}^{e}$ ,  $V_x$ ,  $V_{nt}$ , and  $V_{1ca}^{e}$  measured in dynamic <sup>13</sup>C MRS experiments. Assuming  $V_{y}^{e} = 10 \times V_{yca}^{e}$  and  $V_{n}^{e} = V_{1ca}^{n}$ ; it was possible to assess the composite glial tricarboxylic acid (TCA) cycle flux  $V_{gt}^{e}$  ( $V_{gt}^{e} = V_{tca}^{e}$ /( $V_{y}^{e} + V_{tca}^{e}$ )) and the neurotransmission flux  $V_{nt}$  from <sup>11</sup>C tissue-activity curves obtained within 30 minutes in the rat cortex with a beta-probe after a bolus infusion of [1-<sup>11</sup>C] acetate (*n*=9), resulting in  $V_{gt}^{e} = 0.136 \pm 0.042$  and  $V_{nt} = 0.170 \pm 0.103 \,\mu$ mol/g per minute (mean  $\pm$  s.d. of the group), in good agreement with <sup>13</sup>C MRS measurements. *Journal of Cerebral Blood Flow & Metabolism* (2012) **32**, 548–559; doi:10.1038/jcbfm.2011.162; published online 30 November 2011

**Keywords:** [1-<sup>11</sup>C] acetate; astrocytes; glial metabolism; metabolic modeling; neurotransmission

# Introduction

The brain meets its energetic demands at rest and during activation largely, if not exclusively by oxidative combustion of fuels. The tricarboxylic acid (TCA) cycle is central to oxidative cerebral metabolism and its metabolic rate is thus particularly important to measure when studying brain energetic needs under different physiological conditions. In addition to the generation of energy for brain cells ultimately in the form of high-energy phosphates such as ATP, the TCA cycle is involved in the metabolism of amino acids, such as the major excitatory neurotransmitter glutamate.

The major substrate for brain metabolism is glucose. However, a limitation in the use of labeled glucose or analogs to study brain metabolism is that these tracers must pass through the glycolysis before reaching the TCA cycle and do not reflect directly TCA cycle activity. Deoxyglucose derivates, such as the most frequently used fluorodeoxyglucose (FDG) do not even enter the glycolysis. They are trapped after phosphorylation by hexokinase to (fluorodeoxy)-glucose-6-phosphate and thus cannot reflect oxidative metabolism. A solution is to use a direct TCA cycle precursor, entering the metabolic pathway after the glycolytic branch point. Acetate, which is metabolized to acetyl-CoA and enters the TCA cycle through citrate synthetase, similarly to pyruvate, is an example of such a precursor.

Moreover, the conpartmentation of glutamate metabolism in brain opens the way to *in vivo* studies of neuroglial interaction, using glial- or neuronalspecific substrates, or tracers metabolized simultaneously by both cells. In contrast to glucose, acetate is uniquely metabolized in the glial compartment (Waniewski and Martin, 1998) and turns out to be an ideal substrate to probe glial oxidative metabolism

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and to increase the sensitivity of the measurement of the glutamate-glutamine cycle (de Graaf et al, 2003b; Henry et al, 2006). Labeled with the positron emitting carbon-11, [1-11C] acetate is thus a suitable substrate to assess glial oxidative metabolism and local neurotransmission using positron emission tomography (PET) or beta-probes (Wyss et al, 2009, 2011). However, to date, no metabolic model has been presented to analyze brain [1-<sup>11</sup>C] acetate studies, based on the biochemical reactions involved in acetate utilization (e.g., TCA cycles, glutamate-glutamine cycle). The aim of this study was to develop a kinetic model for brain [1-11C] acetate infusion experiments, based on the modeling methods used for Nuclear Magnetic Resonance spectroscopy, compatible with the analysis of data acquired with PET or beta-probe (Weber et al, 2003). The model was evaluated on experimental data acquired with a betaprobe *in vivo* in rat brains, after an intravenous bolus injection of  $[1-^{11}C]$  acetate.

## Materials and methods

#### **Beta-Probe Measurements**

The metabolic model presented in this study was developed and tested with *in vivo* experimental data from [1-<sup>11</sup>C] acetate infusion studies, obtained from the PET center in Zurich and published elsewhere (Wyss et al, 2009). Data were acquired in urethane anesthetized Sprague-Dawley rats. All animal experiments were approved by the veterinary authorities of the Canton of Zurich and were performed in accordance with their guidelines. The experiments were performed by licensed investigators. Briefly, a dedicated  $\beta$ -scintillator (Swisstrace, Zurich, Switzerland) was carefully inserted into the cortex at a depth of  $\sim 1.4 \,\mathrm{mm}$  below the dura avoiding large blood vessels. With the <sup>11</sup>C nuclide, the probe measures the local radioactivity density of the tissue over time in a detection sphere of  $\sim 2 \,\mathrm{mm}$  of radius yielding tissue-activity curves (Pain et al, 2002).

To measure the arterial input function (AIF) after bolus injection of 230 to 260 MBq of  $[1^{-11}C]$  acetate, an arteriovenous shunt from the right femoral artery to the right femoral vein was used in conjunction with a  $\gamma$  coincidence counter to measure whole blood radioactivity. Data were acquired during a minimum of 20 minutes, both for the AIF and the brain tissue activity. The input function had a time resolution of 2 seconds, while each beta-probe measurement was averaged over 50 seconds.

#### **Standard One-Tissue Compartment Model**

A previous model for brain studies is the one-tissue compartment model originally developed for <sup>11</sup>C-acetate cardiac studies (Buck *et al*, 1991). This model, composed of two pools, is provided for completeness in Figure 1A. The first pool represents acetate radioactivity concentration in the plasma, known as AIF. The second pool represents the total brain tissue activity. This pool is the sum of the activity

**Figure 1** (**A**) One-tissue model of acetate metabolism originally developed for <sup>11</sup>C-acetate cardiac studies (Buck *et al*, 1991). (**B**) Typical result obtained using this model on brain beta-probe data. (**C**) The residuals show an unsatisfactory modeling of the experimental data, suggesting a more complex dynamics. CBV, cerebral blood volume.

concentrations of all labeled metabolites. The rate of label transfer between the two pools is typically calculated from the first-order rate constants  $K_1$  and  $k_2$ , representing the uptake of <sup>11</sup>C-acetate and the clearance of <sup>11</sup>C through the molecules resulting from brain metabolism of acetate (predominantly <sup>11</sup>CO<sub>2</sub>), respectively (Wyss *et al*, 2009).

The measured total activity curve includes the tissue compartment and the vascular compartment. The vascular volume fraction or cerebral blood volume (CBV) in the rat cerebral cortex is on the order of 2% to 3% (Todd *et al*, 1993*a*; Weeks *et al*, 1990). The experimental curve is, therefore, fitted to a linear combination of the two pools:

$$C_{measured}(t) = (1 - \alpha)C_{tissue}(t) + \alpha C_{plasma}(t)$$

where  $\alpha$  corresponds to the relative CBV. Using the measured AIF, the model was fitted to the tissue-activity curve by varying the three parameters  $K_1$ ,  $k_2$ , and  $\alpha$ . The plot in Figure 1C shows a systematic deviation of residuals from zero, which was consistently observed with most experimental data.

#### **Neuroglial Model**

In this study, metabolic modeling was developed using a compartmentalized neurotransmitter approach previously applied in <sup>13</sup>C Nuclear Magnetic Resonance studies (Gruetter *et al*, 2001). Brain tissue is mainly composed of glial and neuronal cells. It is now well accepted that glial cells are actively involved in excitatory neurotransmission,





e.g., through the uptake of the neurotransmitter glutamate from the synaptic cleft (Arriza *et al*, 1994). The model, therefore, consists of two main metabolic compartments corresponding to the two cell types. Each compartment consists of the respective TCA cycle as well as of the glutamate-glutamine cycle, linking the metabolism of both compartments.

Acetate is almost exclusively metabolized in astrocytes (glial compartment) (Lebon *et al*, 2002; Waniewski and Martin, 1998). As a consequence, the inflow of new label from the substrate is occurring only through the glial TCA cycle. Nevertheless, the neuronal TCA cycle rate was accounted for, since it provides unlabeled carbons originating from neuronal pyruvate metabolism to the glutamate-glutamine cycle, which affects overall tissue activity.

The resulting model is presented in Figure 2A. To illustrate how label is transferred within a molecule in the TCA cycle, we added the detailed scheme in Figure 2B. <sup>11</sup>C from [1-<sup>11</sup>C] acetate enters the glial TCA cycle at the position 5 of citrate. Pyruvate metabolism in the glial compartment dilutes the acetyl-CoA pool. In the first turn of the TCA cycle, <sup>11</sup>C reaches the position 5 of 2-oxoglutarate with a total net flux  $K_{dil} \times V_{tca}^{g}$  (Supplementary Appendix A), where  $K_{dil}$  represents the affinity of glial metabolism to acetate.  $K_{\rm dil}$  was fixed to 0.76, as found in <sup>13</sup>C magnetic resonance spectroscopy (MRS) rat studies, in similar physiological conditions (Duarte et al, 2011). 2-Oxoglutarate exchanges label with cytosolic glutamate. This transmitochondrial label exchange, denoted by  $V_{\rm x}^{\rm g}$ transfers label from the carbon position 5 of 2-oxoglutarate to the position 5 of glutamate. Due to the symmetry of the succinate molecule, the second turn of the TCA cycle brings half of the labeled carbons of the position 5 of 2-oxoglutarate to the position 1 of 2-oxoglutarate and half of it is eliminated as  $CO_2$ . Through the transmitochondrial flux  $V_x^{\text{g}}$ , [1-<sup>11</sup>C] glutamate is formed from [1-<sup>11</sup>C] 2-oxoglutarate. In glia, metabolic pathways involving aspartate were assumed to be negligible (Wurdig and Kugler, 1991).

On the neuronal side, label entering the TCA cycle in the first turn from acetate is neglected, consistent with the glial-specific uptake of acetate. Nevertheless, once neuronal glutamate is sufficiently labeled by the action of the glutamate-glutamine cycle  $(V_{nt})$ , the exchange between glutamate and 2-oxoglutarate through  $V_{\rm x}^{\rm n}$  allows in principle a labeling of the glutamate at position 1 from the glutamate at position 5 in the second turn of the TCA cycle. The fractional enrichments (concentration of labeled molecules divided by the total concentration of this molecule in the pool) of the neuronal glutamate pools are expected to be low, because acetate is entering only on the glial side and because the infusion experiments are short (20 minutes in Wyss et al, 2009) on the time scale of neuronal glutamate turnover times. Therefore, the labeling of aspartate through the malate-aspartate shuttle on the neuronal side was assumed to be negligible.

#### **Carbon Dioxide Labeling**

In radiotracer experiments, the measured radioactivity curve represents all labeled compounds. Therefore, the contribution to the total tissue activity of labeled CO<sub>2</sub>, present in high concentrations of ~13.8 to 15.1  $\mu$ mol/g in the brain (Thompson and Brown, 1960; Thompson *et al*, 1980), needs to be additionally taken into account. For the modeling of CO<sub>2</sub> labeling, we assumed a typical value of 15  $\mu$ mol/g of total brain CO<sub>2</sub>, which includes bicarbonate, in rapid exchange with CO<sub>2</sub> due to the action of carbonic anhydrase.

The input of label into the  $CO_2$  pool originates from both glial and neuronal TCA cycles. In fact, two  $CO_2$  molecules are released per turn in the TCA cycle (Figure 2B). An additional  $CO_2$  molecule is produced in the glycolysis for both compartments. Using the metabolic steady-state assumption for  $CO_2$ , the efflux of the  $CO_2$  pool  $V_{out}$  is:

$$V_{\rm out} = 3V_{\rm tca}^{\rm g} + 3V_{\rm tca}^{\rm n}$$

When infusing C1-labeled acetate, the first release of label to CO<sub>2</sub> occurs in decarboxylation of oxalosuccinate in the second TCA cycle turn. Since 2-oxoglutarate can exchange its carbon chain with glutamate, this label loss originates either from acetate or from glutamate C5. The second loss of labeled carbon to CO<sub>2</sub> occurs in decarboxvlation of 2-oxoglutarate, also in the second TCA cycle turn. This labeled carbon can originate directly from an exchange with glutamate C1, from glutamate C5 or acetate. Thus, CO<sub>2</sub> can also be labeled from the neuronal TCA cycle, but only from neuronal glutamate C5 and C1, which both are likely to be only weakly labeled, since acetate does not directly enter neurons. The third CO<sub>2</sub> molecule produced in the glycolysis is unlabeled in both compartments. The relative contribution of each of these pools to CO<sub>2</sub> labeling is elaborated in Supplementary Appendix B.

CO<sub>2</sub> diffuses almost freely across the blood–brain barrier. It was estimated (Supplementary Appendix B) that the total amount of CO<sub>2</sub> in blood, considering all the transport modes (dissolved, buffered with water as bicarbonate, bound to proteins, particularly hemoglobin), is similar to brain CO<sub>2</sub> concentration (Pocock and Richards, 2004). Assuming a fast exchange between these modes compared with brain metabolism (Geers and Gros, 2000) and a cerebral blood flow in the range of 1.3 mL/g per minute (Todd et al, 1993a, b), an influx of 20 µmol/g per minute of unlabeled CO<sub>2</sub> is estimated. This flux is large compared with the TCA cycle fluxes and reduces the <sup>11</sup>CO<sub>2</sub> activity and, therefore, its contribution to the total tissue-activity curve. Including the <sup>11</sup>CO<sub>2</sub> pool introduces an additional differential equation to the existing differential system, but no extra parameter (flux) to adjust.

#### Units of the Data and Derived Fluxes

Positron emission data are measured in kBq/mL and not directly as a concentration (in  $\mu$ mol/g). They are corrected for radioactive decay and delay between the plasma measurement and brain measurement due to blood circulation. The Nuclear Magnetic Resonance metabolic modeling approach expresses the total concentration of metabolites (labeled or not) in  $\mu$ mol/g and the labeling of each chemical pool in terms of fractional or isotopic enrichment

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**Figure 2** (A) Schematic view of the compartmental metabolic model used for brain  $[1-{}^{11}C]$  acetate metabolism. The diagram shows the  ${}^{11}C$  labeling flows from acetate to the positions 5 and 1 of glutamate, glutamine and to CO<sub>2</sub>, through the glial and neuronal tricarboxylic acid (TCA) cycles. (B) Detailed view of the carbon labeling flow through the glial TCA cycle. The neuronal TCA cycle is similar, except that no carbon coming from acetate enters the neuronal TCA cycle. The colors enable the follow-up of the carbons from one molecule to the next. The arrows on the right show how carbons are moving in the carbon chain of 2-oxoglutarate from one TCA cycle turn to the next. The carbons 4 and 5 of citrate are always coming from acetyl-CoA. The carbon positions of glutamate (and glutamine) are identical to those of 2-oxoglutarate. Two carbons are lost in CO<sub>2</sub> at the level of oxalosuccinate and 2-oxoglutarate in each TCA cycle turn.

(Uffmann and Gruetter, 2007). For this study, standard total concentrations of  $3.5 \,\mu$ mol/g for glutamine,  $1 \,\mu$ mol/g for glial glutamate, and  $8 \,\mu$ mol/g for neuronal glutamate were assumed (Kunz *et al*, 2010; Xin *et al*, 2010).

However, a conversion of the data from kBq/mL to  $\mu$ mol/g was not necessary, since we are dealing with linear differential equations (see Supplementary Appendix A) in which both beta-probe data and AIF are given in kBq/mL.

Using absolute concentrations in  $\mu$ mol/g for the chemical pool sizes allows determining metabolic fluxes between the pools in  $\mu$ mol/g per minute from the adjusted rate constants. To solve the differential system, the fractional enrichment of plasma acetate (AIF) was calculated assuming a typical blood acetate concentration of 1  $\mu$ mol/g in the rat (Cetin *et al*, 2003).

#### **Model Analysis**

First, the standard one-tissue compartment model (Figure 1A) was applied to different tissue-activity time courses acquired *in vivo*.

To assess the validity of the suggested new modeling approach, the two-compartmental (neuroglial) model was then implemented and studied under four different sets of assumptions, further described below.

A system of linear differential equations was derived for the neuroglial model, assuming metabolic steady-state (i.e., no net metabolite concentration changes are occurring). As previously shown (Uffmann and Gruetter, 2007), the temporal change of the labeling of the TCA intermediates, present in low concentrations, can be eliminated from the mathematical model without modifying the dynamics of the labeling of glutamate, resulting in a 7-pools model (Glu<sup>g</sup><sub>5</sub>, Glu<sup>1</sup><sub>1</sub>, Gln<sub>5</sub>, Gln<sub>1</sub>, Glu<sup>5</sup><sub>5</sub>, Glu<sup>1</sup><sub>1</sub>, and CO<sub>2</sub>) characterized by five fluxes ( $V^{\rm e}_{\rm tca}$ ,  $V^{\rm g}_{\rm x}$ ,  $V_{\rm nt}$ ,  $V^{\rm tca}_{\rm tca}$ , and  $V^{\rm x}_{\rm x}$ ). The detailed derivation of the labeling equations is provided in Supplementary Appendix A.

The models were developed using Matlab (MathWorks, Natick, MA, USA). To assess the precision and accuracy of the different parameters, Monte-Carlo simulations of the neuroglial model were undertaken, based on the simulated time courses created with the complete model and generated with the following flux values ( $V_{tca}^{g} = 0.06$ ,  $V_{\text{tca}}^{\text{n}} = 0.56, V_{\text{x}}^{\text{g}} = V_{\text{x}}^{\text{n}} = 0.57, \text{ and } V_{\text{nt}} = 0.17 \,\mu\text{mol/g per minute}),$ consistent with human and anesthetized rat brain (Gruetter *et al*, 2001). Gaussian noise (of similar variance  $\sigma^2$  than the one found in experimental beta-probe data) was added to the simulated activity curve, which was then fitted using the different hypotheses described in the scenarios 1 to 4 (see below). Monte-Carlo simulations (500 fits) were undertaken to estimate the uncertainty and mean value of each flux in the different cases. The initial values of the fluxes were taken randomly between 0 and  $1 \mu mol/g$  per minute and the values were constrained to be nonnegative.

The following four scenarios were investigated:

Case 1:  $V_{\text{tca}}^{\text{g}}, V_{\text{x}}^{\text{g}}, V_{\text{nt}}, V_{\text{tca}}^{\text{n}}, V_{\text{x}}^{\text{n}}$  unconstrained. Case 2:  $V_{\text{x}}^{\text{g}} = 10 \times V_{\text{tca}}^{\text{g}}$  and  $V_{\text{x}}^{\text{n}} = V_{\text{tca}}^{\text{n}}$ . Case 3:

as Case 2 but with 5% CBV and  ${}^{11}\text{CO}_2$  contribution added to the simulated experimental curve. A zero weight was given to the data points from the first 2 minutes. *Case 4*:

as Case 3, but the pool of  $\text{CO}_2$  was added to the fitted model.

In Case 3,  $^{11}$ CO<sub>2</sub> production and CBV contribution were added to the simulated tissue-activity curves but not to the model used to fit the data. In this way, the impact of these two additional labeling pools on the estimated fluxes could be investigated.

In Case 4, a sensitivity analysis was also performed to visualize the effect on the tissue curve of varying  $V_{\rm nt}$  and the composite fluxes  $V_{\rm gt}^{\rm s}$  and  $V_{\rm gt}^{\rm n}$  by steps of 10%.  $V_{\rm gt}^{\rm s}$  and  $V_{\rm et}^{\rm n}$  are defined as follows:

$$V_{\text{gt}}^{\text{g}} = \frac{V_{\text{x}}^{\text{g}} V_{\text{tca}}^{\text{g}}}{V_{\text{x}}^{\text{g}} + V_{\text{tca}}^{\text{g}}}$$
 and  $V_{\text{gt}}^{\text{n}} = \frac{V_{\text{x}}^{\text{n}} V_{\text{tca}}^{\text{n}}}{V_{\text{x}}^{\text{n}} + V_{\text{tca}}^{\text{n}}}$ 

The neuroglial model with the assumptions used in Case 4 was finally fitted to nine sets of AIFs and tissue measurements obtained on different rats in resting conditions, under urethane anesthesia (Wyss *et al*, 2009). Mean value and uncertainty of  $V_{\rm nt}$  and the composite TCA fluxes  $V_{\rm gt}^{\rm g}$  and  $V_{\rm et}^{\rm n}$  were estimated with Monte-Carlo simulation.

#### **Results**

#### **Standard One-Tissue Compartment Model**

First, the standard one-tissue compartment model (Figure 1A) was fitted to the measured in vivo tissueactivity time courses. A typical result and fit residual are shown in Figure 1. The contribution of blood activity to the total measured curve was largely limited to the first 2 minutes. After this initial period, the radioactivity originating from blood was close to the experimental noise. For this illustrating example, the signal contribution from blood was estimated by the fit to be  $\alpha = 3.3\%$ , and varied between 2.5% and 5% for all animals. The plot in Figure 1C clearly shows a systematic deviation of residuals from zero, which was consistently observed in most studies, suggesting that the complex dynamics of brain acetate metabolism cannot be fully described by the onetissue compartment model of Figure 1.

#### **Neuroglial Model**

In each case, the mean value of the different fluxes ( $V_{tca}^{g}$ ,  $V_{x}^{g}$ ,  $V_{nt}$ ,  $V_{tca}^{n}$ ,  $V_{x}^{n}$ ,  $V_{gt}^{g}$ , and  $V_{gt}^{n}$ ) is reported (Table 1), as well as their s.d. (calculated from the Monte-Carlo simulations). To check the quality of the fit in the different treated approximations, the fit residual and its s.d. in each case are also indicated.

Table 2 shows the average correlations found for the estimated fluxes in the Monte-Carlo procedure for each case of the four.

**Table 1** Flux values and uncertainties determined by Monte-Carlo simulation

						-										
µmol/g per minute	$\mathbf{V}^{g}_{tca}$	$\Delta V^g_{tca}$	$V_x^g$	$\Delta V_x^g$	$\mathbf{V}_{gt}^{g}$	$\Delta V^g_{gt}$	V <sub>nt</sub>	$\Delta V_{nt}$	$\mathbf{V}_{tca}^{n}$	$\Delta \mathbf{V}_{tca}^{n}$	$\mathbf{V}_x^n$	$\Delta V_x^n$	$\mathbf{V}_{gt}^{n}$	$\Delta V_{gt}^n$	RSS (AU)	$\Delta RSS$ (AU)
Case 1 Case 2	0.314	0.354	0.424	0.370	0.048	0.007	0.455	0.332	0.507	0.274	0.476	0.275	0.189	0.072	11,902 12 315	3,139
Case 3	0.063	0.003	0.633	0.023 0.031	0.054 0.058	0.002	0.450	0.382	0.425 0.475	0.133	0.425	0.133	0.238	0.106	12,313 13,159	3,669
Case 4 True value	$\begin{array}{c} 0.061 \\ 0.060 \end{array}$	0.003	$0.615 \\ 0.570$	0.033	$\begin{array}{c} 0.056 \\ 0.054 \end{array}$	0.003	$\begin{array}{c} 0.488 \\ 0.170 \end{array}$	0.387	$\begin{array}{c} 0.490 \\ 0.560 \end{array}$	0.211	$\begin{array}{c} 0.490 \\ 0.570 \end{array}$	0.211	$\begin{array}{c} 0.245 \\ 0.282 \end{array}$	0.106	13,452 	3,740

Table summarizing the values and uncertainties found in the fit of the simulated data with  $V_{tca}^{g} = 0.06$ ,  $V_{tca}^{n} = 0.56$ ,  $V_{x}^{g} = V_{x}^{n} = 0.57$  and  $V_{nt} = 0.17 \,\mu$ mol/g per minute, under the different constraints (Cases 1 to 4) presented in Materials and methods. To enable a direct comparison between the Cases 1 to 2 and Cases 3 to 4, the residual sum of squares (RSS) was calculated starting from the second minute. The uncertainties were evaluated with Monte-Carlo simulations (500 artificial data).

**Table 2** Correlation between the adjusted metabolic fluxes

Correlation	$\mathbf{V}^{g}_{tca}$	$\mathrm{V}^g_x$	$V_{nt}$	$\mathbf{V}_{tca}^{n}$	$\mathbf{V}_x^n$
(A)					
$V_{\rm tca}^{\rm g}$	1.00	-0.77	-0.11	0.01	-0.01
$V_{\rm x}^{\rm g}$	-0.77	1.00	-0.10	0.08	0.04
$V_{\rm nt}$	-0.11	-0.10	1.00	-0.16	-0.09
$V_{ m tca}^{ m n}$	0.01	0.08	-0.16	1.00	-0.43
$V_{ m x}^{ m n}$	-0.01	0.04	-0.09	-0.43	1.00
Correlation		$\mathbf{V}^{g}_{tca}$	$V_{nt}$	$\mathbf{V}_{tca}^{n}$	
(B)					;
$V_{\rm tca}^{\rm g}$		1.00	-0.4	3	0.37
$V_{\rm nt}$	_	-0.43	1.0	0	-0.19
$V_{ m tca}^{ m n}$		0.37	-0.1	1.00	
( <i>C</i> )					
$V_{ m tca}^{ m g}$		1.00	-0.3	2	0.24
$V_{ m nt}$	_	-0.32	1.0	0	-0.22
$V_{ m tca}^{ m n}$		0.24	-0.2	2	1.00
(D)					
$V_{ m tca}^{ m g}$		1.00	-0.4	7	0.41
$V_{\rm nt}$	-	-0.47	1.0	0	-0.26
$V_{ m tca}^{ m n}$		0.41	-0.2	6	1.00

Correlation of the fitted fluxes in the different simulated scenarios: (A) Case 1, all fluxes unconstrained, (B) Case 2 ( $V_x^g = 10 \times V_{tca}^g$  and  $V_x^n = V_{tca}^n$ ), (C) Case 3 (with cerebral blood volume (CBV) and <sup>11</sup>CO<sub>2</sub> contamination in the measured tissue curve), and (D) Case 4, (like Case 3, CO<sub>2</sub> labeling added to the model).

In the following section, we describe the results summarized in Tables 1 and 2 for each different set of assumptions (Cases 1 to 4).

# Analysis of the Monte-Carlo Simulation for the Four Different Cases

Case 1 (All Five Parameters Unconstrained): The model with five free parameters presented a significant correlation between  $V_{\text{tca}}^{\text{s}}$  and  $V_{\text{x}}^{\text{s}}$  (-0.77), as well as, to a smaller extent, between  $V_{\text{tca}}^{\text{n}}$  and  $V_{\text{x}}^{\text{n}}$  (-0.43; Table 2A), while their respective uncertainties were relatively large (50% to 100%; Table 1).

However, the variance of the corresponding composite fluxes  $V_{gt}^{e}$  and  $V_{gt}^{n}$  was significantly decreased (15% and 38%, respectively).  $V_{nt}$  was uncorrelated and presented an uncertainty of 73%.

Case 2 ( $V_x^{e} = 10 \times V_{tca}^{e}$  and  $V_x^{n} = V_{tca}^{n}$ ): Constraining  $V_x^{e}$  and  $V_x^{n}$  to reduce the uncertainty of neuronal and glial  $V_{tca}$  and  $V_{gt}$  fluxes was without effect on the quality of the fit compared with Case 1, as judged from the fit residual variation, which was within 3%. In addition, the correlation between the fitted fluxes was reduced to < 0.43 in absolute value (Table 2B).

In Case 2, the fitted fluxes were close to the 'true' values (on which the Monte-Carlo simulation is based), except for  $V_{\rm nt}$ , which presented also a high uncertainty (77%). The true  $V_{\rm nt}$  value was within the 95% confidence interval of the estimated  $V_{\rm nt}$ .

Case 3 (with Cerebral Blood Volume and <sup>11</sup>CO<sub>2</sub> Contamination in the Measured Tissue Curve): In Case 3, where CBV and CO<sub>2</sub> contributions were added, the three fitted fluxes showed low correlations <0.32 in absolute value (Table 2C). The uncertainty of  $V_{gt}^{g}$  was particularly low (5%).  $V_{gt}^{n}$  presented a higher uncertainty of ~45%, while  $V_{nt}$  was overestimated and presented a high uncertainty of ~80%. The omission of the two first minutes in the fitting procedure allowed keeping a good fit quality (a fit residual 7% worse compared with Case 2) and similar fitted values, despite the fact that blood activity and <sup>11</sup>CO<sub>2</sub> contributions were not taken into account.  $V_{gt}^{g}$ ,  $V_{nt}$ , and  $V_{gt}^{n}$  differed from their 'true' value by 7%, 173%, and 16%, respectively.

Case 4 (like Case 4,  $CO_2$  Labeling Added to the Model): In Case 4, the activity of the  $CO_2$  pool was added to the fitted curve. A very similar fit residual (residual 9% worse compared with Case 2), flux values and uncertainties were found in Case 4 compared with Case 3.  $V_{gt}^{e}$ ,  $V_{nt}$ , and  $V_{gt}^{n}$  showed a s.d. of 5%, 79%, and 43%, respectively, diverging from the 'true' value by 4%, 187%, and 13%, respectively. These three fluxes were also well uncorrelated (Table 2D), with the strongest correlation of -0.47 between  $V_{tca}^{e}$  and  $V_{nt}$ .

#### Sensitivity Analysis

Figure 3 shows the sensitivity analysis of the neuroglial model to the fitted fluxes, using the assumptions of Case 4. A typical  $[1^{-11}C]$  acetate bolus injection curve was considered as AIF. The analysis was made starting from the typical flux values already used before  $(V_{\rm tca}^{\rm z}=0.06, V_{\rm tca}^{\rm n}=0.56, V_{\rm x}^{\rm g}=V_{\rm x}^{\rm n}=0.57$ , and  $V_{\rm nt}=0.17\,\mu{\rm mol/g}$  per minute). The thick line is the simulated curve with these parameters, while each thinner line represents a step variation of 10% for the considered flux  $(V_{\rm gt}^{\rm g}$  in



**Figure 3** Sensitivity analysis of the model relatively to the parameters  $V_{\rm gt}^{\rm g}$  (**A**),  $V_{\rm nt}$  (**B**), and  $V_{\rm gt}^{\rm n}$  (**C**). The thick line represents the simulated data for ( $V_{\rm tca}^{\rm g} = 0.06$ ,  $V_{\rm tca}^{\rm n} = 0.56$ ,  $V_{\rm x}^{\rm g} = V_{\rm x}^{\rm n} = 0.57$ , and  $V_{\rm nt} = 0.17 \,\mu$ mol/g per minute), using a typical arterial input function. The thinner lines represent each time a step of 10% increase or decrease in the corresponding parameter value. The sensitivity analysis shows that the curve is predominantly driven by the composite flux  $V_{\rm gt}^{\rm g}$ , characterizing the label input in the glial glutamate C5 position.

Figure 3A,  $V_{\rm nt}$  in Figure 3B, and  $V_{\rm gt}^{\rm n}$  in Figure 3C). The result showed that the tissue-activity curve was very sensitive to the glial composite flux  $V_{\rm gt}^{\rm g}$ .  $V_{\rm nt}$  and  $V_{\rm gt}^{\rm n}$  had a much smaller influence on the total brain tissue-activity curve. The low sensitivity of the fitted tissue curve to  $V_{\rm gt}^{\rm n}$  and  $V_{\rm nt}$  was reflected by the relatively large uncertainties found for these fluxes in the Monte-Carlo study.

#### **Experimental Data**

Figure 4 shows a typical fit of an experimental tissueactivity curve obtained with the beta-probe. The assumptions used were those of Case 4, i.e.,  $V_x^g = 10 \times V_{tca}^g$ ,  $V_x^n = V_{tca}^n$  and the two first minutes of experiment were neglected in the fit to minimize CBV contributions to the signal. The goodness of fit is showed by the random distribution of the residual around zero. The experimental data correspond to that presented in Figure 1, where the one-tissue compartment model was fitted.

The neuroglial model was able to characterize the time course, as no discrepancy between experimental data and model was visible. This observation was consistently made for all nine fitted experimental curves.

Figure 5 summarizes the group average and s.d. of fluxes obtained on nine rats in resting conditions. The mean values for  $V_{\rm gt}^{\rm g}$ ,  $V_{\rm nt}$  and  $V_{\rm gt}^{\rm n}$  were, respectively,  $0.136 \pm 0.042$ ,  $0.170 \pm 0.103$ , and  $0.096 \pm 0.075 \,\mu$ mol/g per minute (mean  $\pm$  s.d. of the group). The group average of the flux uncertainties for  $V_{\rm gt}^{\rm g}$ ,  $V_{\rm nt}$ , and  $V_{\rm gt}^{\rm n}$ was, respectively,  $0.004 \pm 0.004$ ,  $0.052 \pm 0.069$ , and



**Figure 4** Fit of the same experimental data as in Figure 3, but using the neuroglial model with the assumption exposed in Case 4. The fit residuals are uniformly distributed around zero. The higher experimental values at the beginning compared with the fit are due to the contamination of the blood activity in brain tissue. However, thanks to the bolus injection of  $[1^{-11}C]$  acetate, this problem can be solved by fitting the curve starting only from minute 2.



**Figure 5** (**A**) Group average and s.d. of fluxes obtained on nine rats in resting conditions. (**B**) Group average of the flux uncertainties obtained on the same nine rats.  $V_{gt}^{g}$  has a reproducible value among the different animals and its uncertainty is low in each individual case, making it a very accurate parameter measured in [1-<sup>11</sup>C] acetate experiments.  $V_{nt}$  is measured with a typical uncertainty of ~30%.

 $0.088 \pm 0.051 \,\mu$ mol/g per minute (mean  $\pm$  s.d. of the group).  $V_{gt}^{g}$  had a reproducible value among the different animals and its uncertainty was low in each individual case, making it a very accurate parameter measured in [1-<sup>11</sup>C] acetate experiments.  $V_{nt}$  was measured with a typical uncertainty of ~30%.

# Discussion

In this study, we built a brain metabolic model for [1-<sup>11</sup>C] acetate infusion experiments based on the radiotracer techniques to measure tissue-activity curves. The modeling approach was based on a twocompartment model typically used in brain <sup>13</sup>C-labeling studies. The sensitivity of the model to the involved biochemical fluxes was assessed by fitting an artificial tissue-activity curve, based on a typical AIF and standard metabolic fluxes. This Monte-Carlo approach based on the simulated data, in which the 'true' flux values are known, allowed a direct assessment of the accuracy and precision of the model under different assumptions. Finally, using the more suitable working assumptions, the model was successfully fitted to nine experimental data sets acquired in vivo from adult rat brain using a beta-probe (Wyss et al, 2009).

# Measurable Fluxes: Unreliability of the Separate $V_x^g$ and $V_{tca}^g$ Estimation

The dynamics of glial glutamate C5 labeling is affected by the composite flux  $V_{\rm gt}^{\rm g}$  and by the

neurotransmission flux  $V_{\rm nt}$ . Hence,  $V_{\rm x}^{\rm g}$  cannot be determined separately from  $V_{tca}^{g}$  when using the glutamate C5 curve only. The labeling dynamics of all the metabolites labeled at C5 is symmetric to the exchange of  $V_x^{\rm g}$  and  $V_{\rm tca}^{\rm g}$  and all pairs of these two fluxes resulting in a same  $V_{gt}^{g}$  will fit identically the C5 metabolites labeling curves (Henry et al, 2006). This underdetermination can be partially removed by additional information coming from the C1labeled metabolites enrichment data. The differential equation related to the labeling of glial glutamate C1 (Supplementary Appendix A, eq. 10) shows that  $V_x^{g}$ and  $V_{tca}^{g}$  act differently on the two precursors of glial glutamate C1 through the glial TCA cycle, namely [1-<sup>11</sup>C] acetate and glial glutamate C5. With a perfect tissue-activity curve, a single pair of  $V_{\rm x}^{\rm g}$  and  $V_{\text{tca}}^{\text{g}}$  would fit properly the data.

However, in radiotracer experiments, the information on C1-labeled metabolites cannot be acquired separately. It is added to the activity from all other labeled metabolites in the tissue. The contribution of the C1 positions to the total tissue activity is low (Figure 4), typically <10%. The separate measurement of  $V_x^{\rm s}$  and  $V_{\rm tca}^{\rm s}$  is thus unreliable, as illustrated by the Monte-Carlo simulation for Case 1 (all fluxes unconstrained). The uncertainties of  $V_x^{\rm s}$  and  $V_{\rm tca}^{\rm s}$  were high and their values remained strongly correlated.

As a consequence, it was more appropriate to fit the experimental data by adjusting  $V_{\text{tca}}^{\text{s}}$  and constraining  $V_{x}^{\text{g}}$  to 10 times the value of  $V_{\text{tca}}^{\text{g}}$ , following the results of several Nuclear Magnetic Resonance studies (Choi *et al*, 2002; Gruetter *et al*, 1992, 2001; Henry *et al*, 2002), while  $V_{\text{gt}}^{\text{g}}$  was reported. A similar approach was used for  $V_{\text{tca}}^{\text{n}}$  and  $V_{x}^{\text{n}}$ , where  $V_{x}^{\text{n}}$  was fixed to the value of  $V_{\text{tca}}^{\text{n}}$ . These constraints were used for the remaining cases, i.e., 2 to 4, which affected the quality of the fit marginally, yet improved the precision on the remaining fluxes ( $V_{\text{gt}}^{\text{g}}$ ,  $V_{\text{nt}}$ , and  $V_{\text{gt}}^{\text{n}}$ ).

The affinity of glial metabolism to acetate, represented by  $K_{dil}$ , could be theoretically extracted from the steady-state enrichment of the glutamine labeling positions. However, due to bolus injection of  $[1-^{11}C]$ acetate, a labeling steady-state was never achieved. As a consequence, including  $K_{dil}$  as free parameter was leading to a high uncertainty on its value. We chose, therefore, to fix  $K_{dil}$  to the value found in <sup>13</sup>C MRS rat studies, in similar physiological conditions (Duarte *et al*, 2011).

#### **Glial Fluxes**

With the aforementioned assumptions for  $V_x$  and  $V_{\text{tca}}$  $(V_x^{\text{g}} = 10 \times V_{\text{tca}}^{\text{g}} \text{ and } V_x^{\text{n}} = V_{\text{tca}}^{\text{n}})$ , the composite glial TCA cycle flux  $V_{\text{gt}}^{\text{g}}$  was determined with high precision in all Cases 2 to 4, with a s.d. of <6% for Case 4. The sensitivity of the measured tissue-activity curve toward  $V_{\text{gt}}^{\text{g}}$  is significant (Figure 3A).

The accuracy of  $V_{gt}^{g}$  was hardly dependent on the working assumptions studied in Cases 2 to 4, varying from 0.054 to 0.058  $\mu$ mol/g per minute for a 'true'

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value of 0.054  $\mu$ mol/g per minute. Therefore,  $V_{gt}^{g}$  is a highly reliable flux when measured with  $[1-1^{11}C]$ acetate.

#### **Neuronal Fluxes**

Using the assumptions that  $V_x^{g} = 10 \times V_{tca}^{g}$  and  $V_x^{n} = V_{tca}^{n}$  (Cases 2 to 4),  $V_{tca}^{g}$ ,  $V_{nt}$ , and  $V_{tca}^{n}$  were adjusted. Despite the goodness of fit,  $V_{\rm nt}$  and  $V_{\rm gt}^{\rm n}$ presented relatively high uncertainties (77% and 45%, respectively) (Table 1, Case 2) due to their low impact on the measured curve, as seen with the sensitivity analysis in Figures 3B and 3C. In acetate infusion experiments, the role played by the neuronal fluxes is limited to dilute the neuronal glutamate C5 pool and by partially labeling neuronal glutamate C1 from glutamate C5. Both of these pools have a low activity throughout the experiment and contribute weakly to the total measured tissue-activity curve (Figure 4). Variations in labeling of these pools are thus imprecisely measured.

In the experimental cases, the value of  $V_{\rm nt}$ impacted the precision of  $V_{gt}^n$  (data not shown): with higher  $V_{\rm nt}$ , the fractional enrichment of the neuronal glutamate positions increased faster and the impact of  $V_{gt}^n$  on the tissue-activity curve was thus stronger, resulting in a higher precision of the fitting procedure on  $V_{gt}^{n}$ . The precision of this flux was thus case dependent.

To analyze the impact of neglecting completely the neuronal dilution in the fit, the simulated data were fitted with neuronal fluxes fixed to  $0 \mu mol/g$  per minute (data not shown). The fit residual was clearly increasing (by 110% compared with Case 2, where  $V_{\text{tca}}^{\text{n}}$  is adjusted);  $V_{\text{nt}}$  diverged from its real value, while the glial fluxes were less affected by this hypothesis. As a consequence, although poorly determined, the neuronal fluxes  $V_x^n$  and  $V_{tca}^n$  should be adjusted during the fit.

#### **Neurotransmission Flux**

 $V_{\rm nt}$  converts glial glutamate-labeling positions to glutamine and eventually to neuronal glutamate. Since the sum of all the activity of these pools is measured, an increase in  $V_{\rm nt}$  generates a faster transit of <sup>11</sup>C through the glutamate-glutamine cycle, without affecting significantly the shape of the total tissue-activity curve (sum of the glutamate and glutamine positions), as can be seen on the sensitivity analysis in Figure 3B.

As a consequence, the fitted value of  $V_{\rm nt}$  had a relatively high uncertainty compared with V<sup>g</sup><sub>gt</sub> (Table 1, Cases 1 to 4). In Case 4,  $V_{\rm nt}$  was not strongly correlated with the neuronal and glial TCA cycle fluxes and has therefore low impact on the value found for  $V_{gt}^{g}$  and  $V_{gt}^{n}$  (Table 2D).

#### **Blood Partial Volume**

As shown in the decomposition of the total tissueactivity curve in Figure 4, the tissue pool dominating

the total labeling in the first minutes is glutamate C5. From its labeling equation (Supplementary Appendix A, eq. 9), it can be seen that the slope of glutamate C5 labeling at early time points is equal to  $V_{\rm gt}^{\rm g} \times K_{\rm dil}$ . As already mentioned in the case of the one-tissue compartment model, the activity contribution due to blood partial volume effect in the measured voxel is mainly limited to the first 2 minutes: fitting the complete tissue-activity curve with a variable blood partial volume would lead to a strong correlation between  $V_{gt}^{g}$  and the blood partial volume, since both are closely related to the first points of the tissue-activity curve (data not shown). These points have also the lowest signal-to-noise ratio of the experiment. As a consequence, CBV values can only be unreliably extracted from the fitting procedure. Likewise, assuming a standard brain blood partial volume value may depend on the position of the probe in the brain and might vary between animals leading to biased  $V_{gt}^{g}$  values.

Therefore, it was preferred to neglect the first 2 minutes of data following the <sup>11</sup>C bolus injection and to neglect the blood partial volume contribution. As a matter of fact, in the simulations of Cases 3 and 4, a 5% blood partial volume contribution was added to the simulated total tissue curve, while the model was fitted starting after the second minute without taking into account the blood contamination. Table 1 Case 3 (with CBV contamination) compared with Case 2 (without CBV contamination) shows that blood contamination of the signal resulted in a slight increase in the fit residual, while this working assumption minimally affected the value and precision of the adjusted fluxes (<8% for  $V_{tca}^{g}$ ,  $V_{x}^{g}$ , and  $V_{\rm nt}$  and 11% for  $V_{\rm tca}^{\rm n}$  and  $V_{\rm x}^{\rm n}$ ). In Case 3, CBV and <sup>11</sup>CO<sub>2</sub> contributions were added simultaneously, to avoid the generation of too many scenarios in the fitting assumptions. Adding only the CBV contribution to the simulated data resulted in similar fluxes values, uncertainties and correlations (not shown).

#### Inclusion of the CO<sub>2</sub> Labeling in the Model

In Case 3, the labeling of  $CO_2$  was also added to the simulated tissue-activity curve but not to the model used. As discussed above regarding the CBV contribution, the fitted flux values were minimally affected by this additional contribution. Adding the  $CO_2$  pool without the CBV contribution to the simulated tissue-activity curve led to the same observation (not shown). This is consistent with the low activity of  ${}^{11}CO_2$  compared with the total tissue activity observed in the fits of the experimental data (Figure 4). As a consequence, the contribution of  $CO_2$  to total tissue activity can be considered negligible.

Adding the  $CO_2$  pool to the fitted model (Case 4) had a positive impact especially on  $V_{gt}^{g}$ , whose value was getting closer to the 'true' value used for the

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simulation. Adding the pool of  $CO_2$  in the model is, therefore, desirable to obtain unbiased quantification of the glial TCA cycle activity, which is the most precisely determined flux of this neuroglial model when using <sup>11</sup>C-acetate beta-probe data. For these reasons, the assumptions used in Case 4 were further used to fit the experimental data and are proposed in general to fit the model presented here to  $[1-^{11}C]$ acetate brain studies.

#### Fluxes Derived from the Experimental In Vivo Data

The model was fitted to nine tissue-activity curves with corresponding AIFs (Figure 4). The consistently uniform distribution of the residuals around zero reflects the good quality of the fit of the model. The precision on  $V_{\text{gt}}^{\text{s}}$ ,  $V_{\text{nt}}$ , and  $V_{\text{gt}}^{\text{n}}$  obtained with the fit of the experimental data with the neuroglial model were of the same order as the results of the Monte-Carlo simulations.

In the experimental results, the group average  $V_{\rm gt}^{\rm n}$  is as large as the corresponding group s.d.  $(V_{\rm gt}^{\rm n}=0.10\,\mu{\rm mol/g}$  per minute,  $\Delta V_{\rm gt}^{\rm n}=0.09\,\mu{\rm mol/g}$  per minute). Therefore, we conclude that  $V_{\rm gt}^{\rm n}$  cannot be reliably extracted from the fit. For  $V_{\rm nt}$ , the average uncertainty is ~30% of the flux value, which makes it a less sensitive flux in [1-<sup>11</sup>C] acetate infusion studies, compared with  $V_{\rm gt}^{\rm g}$ . The average  $V_{\rm nt}$  is in good agreement with the values found in <sup>13</sup>C MRS studies (de Graaf *et al*, 2003*a*; Sibson *et al*, 1997, 2001; Duarte *et al*, 2011).

 $V_{gt}^{g}$ , characterizing glial oxidative metabolism, can be reliably and reproducibly determined with this protocol of [1-<sup>11</sup>C] acetate infusion. The average  $V_{gt}^{g}$  is comparable to the literature values found in <sup>13</sup>C MRS studies (de Graaf *et al*, 2003*a*; Sibson *et al*, 2001; Duarte *et al*, 2011). In some studies,  $V_x$  (assumed identical in the neuronal and glial compartments) was found to be significantly bigger than  $V_{tca}^{g}$ . In this case, the composite flux  $V_{gt}^{g}$  is almost equal to  $V_{tca}^{g}$ . The average  $V_{gt}^{g}$  found in the present study was, therefore, compared with the values of  $V_{tca}^{g}$  of these studies.

The experimental precision on  $V_{gt}^{e}$  found in this study is comparable or even higher than those found with <sup>13</sup>C MRS in the literature. The comparison with <sup>13</sup>C glucose infusion experiments should be performed with care, since the value found in these cases for  $V_{tca}^{e}$  might be subject to high uncertainties (Shestov *et al*, 2007). Glucose being metabolized both on the neuronal and glial sides and  $V_{tca}^{n}$  being typically five times bigger than  $V_{tca}^{e}$ , the labeling of glutamate is mainly reflecting neuronal activity and the data obtained in glucose <sup>13</sup>C MRS studies are much less sensitive to glial metabolism.

In the glial compartment, pyruvate carboxylation affects the position C1 of glial glutamate, as an additional dilution flux, in the second turn of the TCA cycle. However, the C1-labeling positions have a low contribution to the total tissue-activity curve

(Figure 4); and therefore, pyruvate carboxylation affects marginally the <sup>11</sup>C tissue uptake curves. Fitting a tissue-activity curve generated with the inclusion of pyruvate carboxylation, but fitted with the presented model had negligible impact on the derived metabolic fluxes  $V_{gt}^{g}$ ,  $V_{nt}$ , and  $V_{gt}^{n}$  (data not shown). The pyruvate carboxylation pathway was, therefore, neglected in this model.

The flux  $V_{gt}^{s}$  determined with the neuroglial model has a similar role as the uptake parameter  $K_1$ of the previously applied one-tissue compartment model. However, the dynamics of <sup>11</sup>C release from brain tissue is more complex and requires the modeling of the neuroglial interaction. The glutamate-glutamine cycle is buffering <sup>11</sup>C, storing the label temporarily before its release as <sup>11</sup>CO<sub>2</sub> from the glial or neuronal TCA cycle. This delayed <sup>11</sup>C release was already noticed with the one-tissue compartment model.  $k_2$  was decreasing significantly when fitting only the first 5 minutes of the uptake curve compared with the fit of the complete curve (Wyss *et al*, 2009).

Compared with <sup>13</sup>C MRS, the determination of glial oxidative metabolism with [1-<sup>11</sup>C] acetate infusion and positron emission measurements has several advantages. First, the high sensitivity of radiotracer detection enables measuring glial metabolism under physiological conditions due to trace amounts of [1-<sup>11</sup>C] acetate infusion (~0.5 nmol). Second, the experiment can be realized in only 20 to 30 minutes, while <sup>13</sup>C MRS studies, with a typical time resolution of 10 minutes, need at least 2 to 3 hours of acquisition. The spatial resolution of this technique (~8  $\mu$ L with beta-probe) is higher than what can be achieved with <sup>13</sup>C MRS, thanks to the high sensitivity of positron emitter detection.

Using a PET scanner instead of the beta-probe would allow whole brain coverage in a single experiment with less impact on brain tissue, while obtaining similar or better spatial resolution. A cerebral mapping of  $V_{gt}^{e}$  is therefore conceivable, provided a nearby cyclotron is available.

However, the absence of chemical information on the molecule emitting the positron reduces the number of determined metabolic fluxes compared with <sup>13</sup>C MRS. The precise measurement of the AIF and its correction is an important step of the measurement to obtain accurate results and is probably the most limiting factor.

Like in <sup>13</sup>C MRS studies, a measurement of the total plasma acetate is also necessary to further extract the fractional enrichment of acetate, the precursor of all the modeled pools. However, in [1-<sup>11</sup>C] acetate studies, one single measurement should be enough since the injection of the tracer is negligible compared with the natural plasma acetate concentration, which should therefore not vary significantly during the experiment. The requirement is thus similar to an <sup>18</sup>FDG study, in which the plasma glucose concentration is needed for quantification.

#### Conclusion

We conclude that the presented new model for *in vivo* brain metabolic studies using [1-<sup>11</sup>C] acetate infusion is able to describe the kinetics in <sup>11</sup>C-acetate radiotracer as well as <sup>13</sup>C-acetate MRS experiments, allowing to estimate  $V_{\rm gt}^{\rm g}$  and  $V_{\rm nt}$  for the rat in <30 minutes.

We further conclude that radiotracer experiments using [1-<sup>11</sup>C] acetate infusion can be used for the study of local glial oxidative metabolism. Minimal invasiveness and short acquisition periods make it an interesting method for human—possibly clinical—PET applications.

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## Disclosure/conflict of interest

The authors declare no conflict of interest.

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Supplementary Information accompanies the paper on the Journal of Cerebral Blood Flow & Metabolism website (http://www.nature.com/jcbfm)